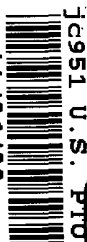


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UTILITY PATENT APPLICATION TRANSMITTAL

(Only for new nonprovisional applications under 37 CFR 1.53(b))

Attorney Docket No.

N0069US

First Inventor

JOSH

Title

Method and System for Wavelet Based
Representation and Use of Cartographic Data

Express Mail Label No.

EF 173 000 843 US

APPLICATION ELEMENTS

See MPEP chapter 600 concerning utility patent application contents

1. ☒ Fee Transmittal Form (e.g., PTO/SB/17)
(Submit an original and a duplicate for fee processing)
2. ☐ Applicant claims small entity status.
See 37 CFR 1.27.
3. ☒ Specification [Total Pages 24]
(preferred arrangement set forth below)
 - Descriptive title of the invention
 - Cross Reference to Related Applications
 - Statement Regarding Fed sponsored R & D
 - Reference to sequence listing, a table, or a computer program listing appendix
 - Background of the Invention
 - Brief Summary of the Invention
 - Brief Description of the Drawings (if filed)
 - Detailed Description
 - Claim(s)
 - Abstract of the Disclosure
4. ☒ Drawing(s) (35 U.S.C. 113) [Total Sheets 4]
5. Oath or Declaration [Total Pages 2]
 - a. ☒ Newly executed (original or copy)
 - b. ☐ Copy from a prior application (37 CFR 1.63 (d))
(for continuation/divisional with Box 17 completed)
 - i. ☐ **DELETION OF INVENTOR(S)**
Signed statement attached deleting inventor(s)
named in the prior application, see 37 CFR
1.63(d)(2) and 1.33(b).
6. ☐ Application Data Sheet. See 37 CFR 1.76

ADDRESS TO:

Assistant Commissioner for Patents
Box Patent Application
Washington, DC 20231

7. ☐ CD-ROM or CD-R in duplicate, large table or
Computer Program (Appendix)
8. Nucleotide and/or Amino Acid Sequence Submission
(if applicable, all necessary)
 - a. ☐ Computer Readable Form (CRF)
 - b. Specification Sequence Listing on:
 - i. ☐ CD-ROM or CD-R (2 copies); or
 - ii. ☐ paper
 - c. ☐ Statements verifying identity of above copies

ACCOMPANYING APPLICATION PARTS

9. ☒ Assignment Papers (cover sheet & document(s))
10. ☐ 37 CFR 3.73(b) Statement ☐ Power of
(when there is an assignee) Attorney
11. ☐ English Translation Document (if applicable)
12. ☐ Information Disclosure ☐ Copies of IDS
Statement (IDS)/PTO-1449 Citations
13. ☐ Preliminary Amendment
14. ☒ Return Receipt Postcard (MPEP 503)
(Should be specifically itemized)
15. ☐ Certified Copy of Priority Document(s)
(if foreign priority is claimed)
16. ☐ Other:

17. If a CONTINUING APPLICATION, check appropriate box, and supply the requisite information below and in a preliminary amendment, or in an Application Data Sheet under 37 CFR 1.76:

☐ Continuation ☐ Divisional ☐ Continuation-in-part (CIP)

of prior application No.: _____ / _____

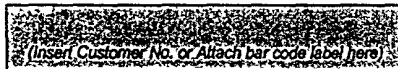
Prior application information:

Examiner: _____

Group / Art Unit: _____

For CONTINUATION OR DIVISIONAL APPS only: The entire disclosure of the prior application, from which an oath or declaration is supplied under Box 5b, is considered a part of the disclosure of the accompanying continuation or divisional application and is hereby incorporated by reference. The incorporation can only be relied upon when a portion has been inadvertently omitted from the submitted application parts.

18. CORRESPONDENCE ADDRESS

☐ Customer Number or Bar Code Label

or



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Registration No. (Attorney/Agent)

32,908

Signature

Date Nov. 6, 2000

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**FEE TRANSMITTAL
for FY 2001**

Patent fees are subject to annual revision.

Complete if Known

Application Number	
Filing Date	11/6/00
First Named Inventor	JOSHI
Examiner Name	
Group Art Unit	
Attorney Docket No.	N006905

TOTAL AMOUNT OF PAYMENT

(\$ 1196.00)

METHOD OF PAYMENT

- 1.
- ☒
- The Commissioner is hereby authorized to charge indicated fees and credit any overpayments to.

Deposit Account Number	50 0728
Deposit Account Name	Navigation Technologies

☒ Charge Any Additional Fee Required
Under 37 CFR 1.16 and 1.17☐ Applicant claims small entity status.
See 37 CFR 1.27

- 2.
- ☐
- Payment Enclosed:

☐ Check ☐ Credit card ☐ Money Order ☐ Other**FEE CALCULATION****1. BASIC FILING FEE**

Large Entity		Small Entity		Fee Description	Fee Paid
Fee Code	Fee (\$)	Fee Code	Fee (\$)		
101	710	201	355	Utility filing fee	710
106	320	206	160	Design filing fee	
107	490	207	245	Plant filing fee	
108	710	208	355	Reissue filing fee	
114	150	214	75	Provisional filing fee	

SUBTOTAL (1) (\$ 710-)**2. EXTRA CLAIM FEES**

Total Claims	Extra Claims	Fee from below	Fee Paid
27	-20** = 7	18	126
7	-3** = 4	86	320
Multiple Dependent			

Large Entity		Small Entity		Fee Description
Fee Code	Fee (\$)	Fee Code	Fee (\$)	
103	18	203	9	Claims in excess of 20
102	80	202	40	Independent claims in excess of 3
104	270	204	135	Multiple dependent claim, if not paid
109	80	209	40	** Reissue independent claims over original patent
110	18	210	9	** Reissue claims in excess of 20 and over original patent

SUBTOTAL (2) (\$ 446-)

**or number previously paid, if greater; For Reissues, see above

FEE CALCULATION (continued)**3. ADDITIONAL FEES**

Large Entity		Small Entity		Fee Description	Fee Paid
Fee Code	Fee (\$)	Fee Code	Fee (\$)		
105	130	205	65	Surcharge - late filing fee or oath	
127	50	227	25	Surcharge - late provisional filing fee or cover sheet	
139	130	139	130	Non-English specification	
147	2,520	147	2,520	For filing a request for <i>ex parte</i> reexamination	
112	920*	112	920*	Requesting publication of SIR prior to Examiner action	
113	1,840*	113	1,840*	Requesting publication of SIR after Examiner action	
115	110	215	55	Extension for reply within first month	
116	390	216	195	Extension for reply within second month	
117	890	217	445	Extension for reply within third month	
118	1,390	218	695	Extension for reply within fourth month	
128	1,890	228	945	Extension for reply within fifth month	
119	310	219	155	Notice of Appeal	
120	310	220	155	Filing a brief in support of an appeal	
121	270	221	135	Request for oral hearing	
138	1,510	138	1,510	Petition to institute a public use proceeding	
140	110	240	55	Petition to revive - unavoidable	
141	1,240	241	620	Petition to revive - unintentional	
142	1,240	242	620	Utility issue fee (or reissue)	
143	440	243	220	Design issue fee	
144	600	244	300	Plant issue fee	
122	130	122	130	Petitions to the Commissioner	
123	50	123	50	Petitions related to provisional applications	
126	240	126	240	Submission of Information Disclosure Stmt	
581	40	581	40	Recording each patent assignment per property (times number of properties)	40
146	710	246	355	Filing a submission after final rejection (37 CFR § 1.129(a))	
149	710	249	355	For each additional invention to be examined (37 CFR § 1.129(b))	
179	710	279	355	Request for Continued Examination (RCE)	
169	900	169	900	Request for expedited examination of a design application	

Other fee (specify) _____

* Reduced by Basic Filing Fee Paid

SUBTOTAL (3) (\$ 40-)**SUBMITTED BY****Complete (if applicable)**

Name (Print/Type)	Frank J. Kozak	Registration No. (Attorney/Agent)	32,908	Telephone	847/795-7371
Signature	<i>Frank J. Kozak</i>	Date	Nov. 6, 2000		

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IN THE UNITED STATES PATENT AND TRADEMARK OFFICE
APPLICATION FOR UNITED STATES PATENT

INVENTOR: RAJASHRI JOSHI

TITLE: METHOD AND SYSTEM FOR WAVELET-
BASED REPRESENTATION AND USE OF
CARTOGRAPHIC DATA

ATTORNEYS: Frank J. Kozak
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METHOD AND SYSTEM FOR WAVELET-BASED REPRESENTATION AND USE OF CARTOGRAPHIC DATA

5

TECHNICAL FIELD OF THE INVENTION

The present invention relates generally to cartography, and in particular, to the use of wavelet transforms to represent cartographic data.

10

BACKGROUND OF THE INVENTION

Cartographic databases are used in computer-based systems to represent geographic features on displayable maps. These geographic features may include roads, intersections, and points-of-interest, as well as other features, such as lakes, railroad tracks, buildings, airports, stadiums, parks, mountain ranges, bridges, and so on. To permit these features to be displayed, cartographic databases usually include geographic location information in a format that allows computers to display maps illustrating the size, shape, position, and character of these various geographic features on a display device.

In order to represent these continuous features on a computer, it is necessary utilize some form of discretization. Typically, the features are represented in terms of discrete data points consisting of coordinate pairs (longitude, latitude) or coordinate triples (longitude, latitude, altitude). A point feature such as a point of interest or intersection is then represented as a single data point, while other features such as roads, lake boundaries, and so on are represented as a sequence of data points. The endpoints of the geographic features are commonly referred to as nodes while data points between the nodes are referred to as shape points. Accordingly, nodes and shape points can be used to approximate the true shape of the geographic feature. The shape points and nodes are stored in what is known as a shape point database, which may be part of a larger cartographic database. With this representation scheme, the spacing between shape points is selected such that the error between the data point representation and the actual geographic feature lies within some acceptable bound. In order to achieve a high level of accuracy and detail in the data point representation, it is often necessary to store a large number of data points.

A function available with some computerized map display systems is the ability to zoom. Zooming is the process of magnifying or reducing the scale of a map displayed on the monitor to change the level of detail. Reducing the display scale in a displayed map is referred to as zooming out, while increasing the display scale is referred to as zooming in.

To permit zooming, some cartographic databases include separate collections of location data, each with a different level of detail, which can be used by the map display function. Using these different layers of cartographic data, the map display function can provide or support zooming. However, providing multiple layers of cartographic data requires additional database storage space.

In one type of display system, the different resolution layers of cartographic data are produced by using line generalization algorithms (also referred to as line simplification algorithms). Many different line generalization algorithms are currently being used in cartography, one of which is the Douglas-Peucker algorithm. Generally, line generalization refers to a process of reducing the data points representing a linear geographic feature in a map, while maintaining the overall shape and/or trend of the feature. By applying a line generalization algorithm to a cartographic database having a large number of data points representing a high level of detail, lower resolution databases can be generated. Although known line generalization algorithms are adequate for producing cartographic data collections with different levels of detail, there is an opportunity to improve upon the speed and efficiency at which the algorithms operate.

Accordingly, there is a need for a method and system for representing cartographic data that improves upon known generalization and zooming techniques and provides an ability to reduce the storage requirements of the data without sacrificing feature resolution.

BRIEF DESCRIPTION OF THE DRAWINGS

FIG. 1 is a Cartesian graph showing a Haar basis function and scaling function.

FIG. 2 is series of Cartesian graphs illustrating an exemplary square integrable function $f(x)$ and its approximation at successively higher resolutions using wavelet basis functions of successively higher resolutions.

FIG. 3 shows a pair of graphs illustrating an exemplary wavelet basis function and the corresponding wavelet scaling function.

FIG. 4 is a block diagram illustrating an exemplary system for converting shape point data of a cartographic database into a database of wavelet and scaling coefficients in accordance with an embodiment of the present invention.

FIG. 5 is a flow chart illustrating a method of operating the processor shown in FIG. 4.

FIG. 6 is a block diagram illustrating a computer-based system capable of displaying cartographic data represented using wavelets in accordance with a further embodiment of the present invention.

FIG. 7 is a flow chart illustrating a method of operating the computer-based system shown in FIG. 6.

FIG. 8 is a block diagram illustrating a system for computing multi-resolution error metrics in accordance with another embodiment of the present invention.

FIG. 9. is a flow chart illustrating a method of operating the processor shown in FIG. 8.

DETAILED DESCRIPTION OF THE PRESENTLY PREFERRED EMBODIMENT(S)

To address the needs for reducing cartographic database sizes and, improving upon known line generalization and zooming techniques, the present invention provides a method and system for generating and using wavelet representations of cartographic data.

The wavelet transform maps a square integrable function to the scale-space domain. Specifically, the wavelet transform of a signal provides information about the resolution content of a function as well as information about the location of each resolution component. This property of wavelets is called time-frequency localization. Wavelet transforms are widely used for the analysis of non-stationary signals. Their unique properties make them a valuable tool in a wide variety of areas such as numerical analysis, edge detection in images, image compression, and analysis of fractal signals, to name just a few.

A wavelet representation of cartographic data can provide an accurate representation of the data, and a consistent and intuitive method for generalization for the purpose of map display at different zoom levels. Furthermore, the wavelet transform can be easily extended to two or more dimensions.

Display operations like generalization and zooming can be accomplished much more intuitively and easily using the wavelet representation, because generalization will simply involve dropping wavelet coefficients at certain scales. With a wavelet representation, the wavelet coefficients for each geographic feature can be stored for the highest level of resolution. To produce displays of lower resolution, higher resolution wavelet coefficients are not used.

Wavelets and Wavelet Transforms

Wavelets are families of functions of the following form

$$\psi_{ab}(x) = |a|^{-1/2} \psi\left(\frac{x-b}{a}\right) \quad (1)$$

where a and b are respectively called the dilation (scaling) and translation parameters. As a is increased, the function $\psi_{ab}(x)$ becomes more spread out or dilated, and as b is increased or decreased $\psi_{ab}(x)$ is shifted or translated by b/a . Thus, wavelets are constructed by dilating and translating a single prototype function $\psi(x)$ called a mother wavelet. The dilation and translation parameter pairs (a, b) can range over a continuous or discrete subset of $\mathbb{R}^+ \times \mathbb{R}$.

If the parameters a and b are restricted such that $a = 2^{-m}$ and $b = mi$, where m and i are integers, then the resulting wavelets are called dyadic wavelets and are parameterized by the integers m and i . Dyadic wavelets are expressed as:

$$\psi_{mi}(x) = 2^{m/2} \psi(2^m x - i) \quad (2)$$

In this case, negative values of m correspond to dilating $\psi(x)$ and positive values of m correspond to contracting $\psi(x)$.

Although the present invention is not so limited, the embodiments described herein can utilize dyadic wavelets. It is possible to select a dyadic mother wavelet $\psi(x)$ such that the set of

functions $\{\psi_{mi}\} \forall (m,i) \in Z \times Z$ constitutes an orthonormal basis for $L^2(\mathcal{R})$, where

$L^2(\mathcal{R})$ represents the space of square-integrable functions defined on the real line. The simplest choice of $\psi(x)$ which yields an orthonormal basis of $L^2(\mathcal{R})$ is the Haar mother wavelet, shown in the FIG. 1.

5 Other orthogonal bases include the Daubechies family of bases. These functions are indexed by an integer N ; the regularity (which loosely means smoothness) of these bases increases with N .

Turning now to wavelet transforms, which rely on wavelets such as those discussed above, there are many different types of wavelet transforms. The wavelet representation of geographic features yields accurate results, and can also be made more accurate by using smoother basis functions, and using more coefficients in certain regions of each geographic feature.

The different types of wavelet transforms are distinguished from one another by the types of wavelets used in their definitions. In the methods and systems disclosed herein, orthonormal wavelet transforms are preferably used; however, nonorthonormal wavelets could also be used for the purpose of representing cartographic data. The semi-discrete orthonormal wavelet transform of a square integrable computable function $f(x)$ is defined, using dyadic wavelets, by the analysis and synthesis equations given below:

20 Analysis Equation:

$$F(m,i) = \int_{-\infty}^{\infty} f(x) \psi_{mi}(x) dx \quad (3)$$

Synthesis Equation:

25

$$f(x) = \sum_{m=-\infty}^{\infty} \sum_{i=-\infty}^{\infty} F(m,i) \psi_{mi}(x) \quad (4)$$

The values $F(m, i)$ are called the wavelet coefficients. The functions

$\psi_{mi}(x) = 2^{m/2} \psi(2^m x - i)$ are the wavelet basis functions. The set of basis functions $\{\psi_{mi}(x)\}$ is thus constructed by scaling and translating the mother wavelet function $\psi(x)$. The integer m is the dilation or scaling parameter and the integer i is a translation parameter. Negative values of m correspond to dilating $\psi(x)$ and positive values of m correspond to contracting $\psi(x)$.

As can be seen from the analysis equation above, the wavelet coefficients $F(m, i)$ are obtained via an inner product computation of the square integrable function $f(x)$ and the corresponding wavelet basis function, i.e., $\langle f(x), \psi_{mi}(x) \rangle$. The set of wavelet coefficients $\{F(m, i)\}$ can be indexed by both scale or resolution m and location or translation i .

The square integrable function $f(x)$ can be reconstructed using the synthesis equation, which is sometimes called a wavelet series expansion. The wavelet representation of a square integrable function is thus a weighted sum of wavelet basis functions, the weights being the wavelet coefficients.

The wavelet transform is considered to be semi-discrete because it takes the continuous function $f(x)$ and transforms it into a set of coefficients indexed by integral values. This transform therefore accomplishes the goal of representing the continuous function $f(x)$ in terms of a set of discrete values $\{F(m, i)\}$, which can be stored in memory on a computer.

The limits on the translation index i in the inner summation of Equation (4) are determined by the support of the square integrable function $f(x)$. The limits on i are finite if $f(x)$ has compact support. The limits on the dilation index m in the outer summation of Equation (4) are infinite. In practice, however, the limits of m must be truncated both above and below to predetermined values to yield a reasonable approximation of $f(x)$. This is done by collecting all terms in the expansion for $m \in (-\infty, M')$ into a single term $\Lambda_{M'}(x)$, which represents the approximation of the function at the highest resolution level, layer 0. The finer details of the function are expressed in terms of a wavelet series expansion as indicated in Equation (5).

$$f(x) \approx \Lambda_{M'}(x) + \sum_{m=M'}^M \sum_{i=-\infty}^{\infty} F(m,i) \psi_{mi}(x) \quad (5)$$

It is often convenient to include only nonnegative scales in the approximation, i.e., truncate all expansion terms below $m = 0$ and above some arbitrary scale M that yields an approximation to $f(x)$ that is acceptable for the given application. Furthermore, $\Lambda_{M'}(x)$ is expressed in terms of dilations and translations of the function $\psi(x)$, which is called the scaling function associated with the wavelet function $\phi(x)$. This results in the following equation:

$$f(x) \approx \sum_{i=-\infty}^{\infty} F'(i) \phi_{M'i}(x) + \sum_{m=M'}^M \sum_{i=-\infty}^{\infty} F(m,i) \psi_{mi}(x) \quad (6)$$

where the quantities the $F'(i)$, are known as the scaling coefficients, and are given by

$$F'(i) = \int_{-\infty}^{\infty} f(x) \phi_{M'i}(x) dx \quad (7)$$

One advantage of using the wavelet transform for representing cartographic data is that the transform organizes the information in the data into components at various resolutions or scales. This is particularly useful for line generalization that supports map display features, such as zooming. This can be explained as follows. For negative values of m , the corresponding wavelet basis functions are dilated, i.e., they have a larger width of support than the mother wavelet. As a result, the wavelet coefficients indicated by negative values of m will correspond to coarse scale or low-resolution information contained in the cartographic data. This corresponds roughly to zooming out and observing the square integrable function $f(x)$ from a distance. The more negative the value of m , the more the displayed feature is effectively zoomed out.

On the other hand, for positive values of m , the resulting wavelet basis functions are contracted with respect to the mother wavelet, i.e., their width of support is smaller than that of the mother wavelet. As a result, the wavelet coefficients indicated by positive values of m correspond to fine scale or high resolution information contained in the cartographic data represented by the square integrable function $f(x)$. This corresponds roughly to zooming in and observing the square integrable function $f(x)$ from close up.

This zooming aspect of wavelet transforms is illustrated in FIG. 2 using the Haar basis function. The column of graphs on the right-hand side of FIG. 2 shows an exemplary square integrable function $f(x)$ and its approximation at successively higher resolutions using wavelet basis functions of successively higher resolutions. The corresponding wavelet basis functions for the successive levels of resolution are illustrated in the left-hand column of graphs.

From the sequence of graphs, it is apparent that as each successive scale of wavelet coefficients is added to the approximation, the approximation becomes more accurate. The Haar basis function is used here only for illustrative purposes. There exist other wavelet bases that can yield accurate representation of continuous functions.

FIG. 3 shows a pair of graphs illustrating an exemplary wavelet basis function and an exemplary wavelet scaling function. The wavelet basis function shown in FIG. 3 is a Daubechies sixth order basis function. This is an orthonormal basis function that has compact support and has a high enough order of continuity for accurately representing cartographic data for some applications. The wavelet scaling function shown in FIG. 3 is associated with the Daubechies sixth order basis function. The Haar basis function is a degenerate case of Daubechies basis function. Daubechies bases do not have closed form expressions, but since all wavelet basis functions are derived from a single prototype function, it is sufficient to compute the values of the mother wavelet once and then store them in a look-up table. There also exist other (non-compactly supported) orthonormal wavelet bases, such as the Battle-Lemarie basis function, which can also be used in other embodiments of the invention.

Other wavelet bases include compactly supported non-orthogonal wavelet bases, such as the B-wavelets which are constructed from splines. The Haar basis function is a degree zero B-spline. These may be of special interest in cartographic applications; however, since they are not orthogonal, the wavelet coefficients will not be quite as easy to compute, as compared to the orthonormal case. However, this is generally not an issue since the wavelet coefficients for a cartographic database need only be computed once, at the time the wavelet database is generated.

Parameterization of Cartographic Data

Each geographic feature can, in general, be represented as a continuous function in space and can be represented in implicit form as $f(x, y, z) = 0$, where x , y and z represent longitude, latitude and altitude, respectively. In order to apply the wavelet transform, it is convenient to express each geographic feature in parametric form as a group $\mathbf{p}(t)$ of polynomial functions of an independent parameter t as follows:

$$\mathbf{p}(t) = [x(t) \quad y(t) \quad z(t)] \quad (8)$$

The parameterization scheme can be chosen in such a way that each of the functions $x(t)$, $y(t)$ and $z(t)$ are each single valued. The wavelet transform can then be applied to each of the functions $x(t)$, $y(t)$ and $z(t)$. This yields $\mathbf{P}(m, i) = [X(m, i) \quad Y(m, i) \quad Z(m, i)]$ where $X(m, i)$, $Y(m, i)$ and $Z(m, i)$ are the wavelet coefficients of $x(t)$, $y(t)$ and $z(t)$ respectively, and $\mathbf{P}'(i) = [X'(i) \quad Y'(i) \quad Z'(i)]$ where $X'(i)$, $Y'(i)$ and $Z'(i)$ are the scaling coefficients of $x(t)$, $y(t)$ and $z(t)$, respectively.

System Architecture

FIG. 4 illustrates an exemplary system 20 for converting a shape point database into a database of wavelet and scaling coefficients in accordance with an embodiment of the present invention. The shape point database itself may be part of a larger cartographic database, which may include other kinds of databases used for functions such as route calculation, maneuver generation, and other navigational functions. The system 20 includes a processor 22 in

communication with a shape point database (DB) 24 and a wavelet database 26. A user interface 21 permits database developers to configure conversion parameters used by the processor 22 such as the desired highest level of resolution in the wavelet representation.

The shape point database 24 stores a plurality of shape points and nodes representing one or more geographic features that can be displayed by a computer-based system, such as a navigation system, as part of a digital map. Shape points and nodes represent geographic locations within a map. In the embodiments disclosed herein, the shape points and nodes can consist of coordinate triples (longitude, latitude, altitude) or coordinate pairs (longitude, latitude), which represents specific locations along geographic features. Nodes are special cases of shape points, representing, for example, intersections between road segments and end points of geographic features.

Data stored in the shape point database 24 can be organized on a per geographic feature basis, i.e., each geographic feature is represented as sequence of nodes and shape points. Although the database 24 can store a number of geographic feature entities 30, three entities SEG_0 , SEG_1 , SEG_2 are shown for illustration purposes. A pair of nodes and zero or more shape point entries 31 can be associated with each entity. For entities representing straight or substantially straight geographic features, the nodes 33 are sufficient to accurately represent the feature; and therefore, for straight geographic features, the nodes alone can be stored without shape points.

In the example shown, a first geographic feature SEG_0 is represented by shape points $SP_0(0) - SP_0(i)$, where i is an integer, and nodes $EN_0(0) - EN_0(1)$; a second feature SEG_1 is represented by shape points $SP_1(0) - SP_1(j)$, where j is an integer, and nodes $EN_1(0) - EN_1(1)$; and a third feature SEG_2 is represented by shape points $SP_2(1) - SP_2(k)$, where k is an integer, and nodes $EN_2(0) - EN_2(1)$.

The processor 22 can be any computing device for performing the steps shown in the flow chart 50 of FIG. 5, including a conventional personal computer (PC) executing a software program. In such an embodiment, the software program can be stored on a computer-usable medium for configuring the processor 22 to perform the method of FIG. 5 as disclosed herein. The computer-usable medium can be any article of manufacture for storing computer programs, such as a CD ROM, hard drive, DVD, diskette, solid-state memory such as a RAM, ROM, or

EEPROM, or the like. Alternatively, the processor 22 can be a custom hardware device, such as one or more application specific integrated circuits (ASIC) designed to perform according to the method shown in FIG. 5.

As will be discussed in greater detail below, the processor 22 processes data stored in the shape point database 24 to convert it into a plurality of wavelet coefficients that are stored in the wavelet database 26. The wavelet representation can provide a more efficient representation of map data that facilitates line generalization and map display features, such as zooming.

Generally, for each geographic feature entity in the shape point database, the processor 22 generates a corresponding set of wavelet and scaling coefficients that are stored in the wavelet database 26. The geographic features can be reconstructed using the wavelet synthesis equation to draw the features on a map display. Further, the wavelet and scaling coefficients for each entity can be indexed by layer or resolution level.

In the example shown, the first geographic feature SEG_0 is represented by wavelet coefficients $P_0(0,0), \dots, P_0(M_0, N_0)$, and scaling coefficients $P'_0(0), \dots, P'_0(N_0)$, where M_0 and N_0 are integers; the second geographic feature SEG_1 is represented by wavelet coefficients $P_1(0,0), \dots, P_1(M_1, N_1)$ and scaling coefficients $P'_1(0), \dots, P'_1(N_1)$, where M_1 and N_1 are integers; and the third geographic feature SEG_2 is represented by wavelet and scaling coefficients $P_2(0), \dots, P_2(N_2)$, where M_2 and N_2 are integers. In the above,

$$P_k(m,i) = [X_k(m,i) \ Y_k(m,i) \ Z_k(m,i)] \text{ and } P'_k(i) = [X'_k(i) \ Y'_k(i) \ Z'_k(i)]. \quad (9)$$

The shape point and wavelet databases 24 and 26, as well as all other databases disclosed herein, can be stored using any suitable computer-usable storage media, such as one or more CD ROMs, hard drives, DVDs, diskettes, solid-state memories such as RAMs, ROMs, or EEPROMs, or the like.

FIG. 5 shows a flow chart 50 illustrating a method of operating the processor 22 shown in FIG. 4. In step 52, the processor 22 receives shape points and/or nodes representing one or more geographic features from the shape point database 24. The processor can include a memory (not shown) for buffering the shape points.

Next in step 56, the wavelet coefficients are computed for each parameterized geographic feature $\mathbf{p}(t) = [x(t) \ y(t) \ z(t)]$. This can be done in one of two possible ways. If $\mathbf{p}(t)$ is known at all points, or if the data points of $\mathbf{p}(t)$ are spaced sufficiently closely, then the wavelet and scaling coefficients are computed for the given data points by using the following discretized versions of Equations (3) and (7):

$$F(m, i) \approx \sum_{k=-\infty}^{\infty} f(k\Delta x) \psi_{mi}(k\Delta x) \Delta x \quad (10)$$

$$F'(i) \approx \sum_{k=-\infty}^{\infty} f(k\Delta x) \phi_{mi}(k\Delta x) \Delta x \quad (11)$$

If the data points of $\mathbf{p}(t)$ are not spaced sufficiently closely, then the wavelet coefficients can be computed by using a least squares fitting technique.

Many different types of wavelet transforms are available and the present invention is not limited to any particular type. However, a preferable form of the wavelet transform employed by the method shown in FIG. 5 was described above in connection with Equations (3)-(4).

An advantage of the wavelet representation of a function is that the wavelet and scaling coefficient set often contains a large number of small or zero values, which can simply be dropped. This allows cartographic data being represented by wavelets to be compressed, reducing the amount of database space necessary to store the wavelet coefficients, without significantly degrading the accuracy of the representation.

In step 58, the wavelet coefficients and scaling coefficients for the geographic features are stored in the wavelet database 26.

FIG. 6 illustrates a computer-based system 100 capable of displaying cartographic data represented using wavelets in accordance with another embodiment of the present invention. The system 100 includes a computer 102, a wavelet database (DB) 104, a user interface 108, and an output display device 106.

The computer 102 can be any computing device, including a conventional PC or other microprocessor-based device having a processor 112 and a memory 110. The processor 112 can execute a computer software program stored in the memory 110. The software program can direct the processor 112 to perform the steps shown in the flow chart diagram 120 of FIG. 7.

The user interface 108 can be a software-generated graphical interface included in a commercially-available PC operating system, configured to direct the processor 112 to receive and process user selections, such as the desired level of resolution in the displayed map.

The wavelet database 104 includes the wavelet coefficients and scaling coefficients and basis function data.

The computer-based system 100 of FIG. 6 can be part of a navigation system included with on-road vehicles, such as automobiles, trucks, buses, and so on, as well as advanced driver assistance systems (ADAS) provided in on-road vehicles.

The flow chart diagram 120 in FIG. 7 illustrates the operation of the computer-based system 100 shown in FIG. 6. In step 122, the computer 102 receives a user selected resolution level from the user interface 108. The resolution level determines the scale at which the cartographic data is displayed, and may be embodied as a zooming feature of the system 100. The zooming feature is described in further detail below.

Next, in step 124, the processor 112 retrieves wavelet and scaling coefficients corresponding to the desired geographic features from the wavelet database 104. The wavelet coefficients in the database 104 can be indexed by scale, facilitating retrieval of the coefficients corresponding to the user selected resolution level, if desired. In addition to retrieving the wavelet coefficients, the processor can also retrieve from the database 54 the precomputed wavelet basis and scaling function values. The parameterized functions

$\mathbf{p}(t) = [x(t) \ y(t) \ z(t)]$, which represent geographic features, such as a road segments, rivers, or the like, for cartographical applications, can be reconstructed from the wavelet coefficients and a look-up table storing the precomputed wavelet basis and scaling function values.

In step 126, the processor 112 reconstructs the functions that represent geographic features. Through a conventional display interface card (not shown), the processor 112 then passes the reconstructed functions to the output display device 106, which then displays the function representing the geographic feature to the user (step 128). The wavelet zooming feature of the system 100 is explained as follows. Starting with the highest resolution wavelet series approximation of the function $\mathbf{p}(t) = [x(t) \ y(t) \ z(t)]$, zooming out, or reducing resolution, can be accomplished by successively removing the finest scale wavelet coefficients from the wavelet expansion. As an example, suppose that the cartographic display data is organized into five layers, labeled layer 0 through layer 4, with layer 0 representing the lowest level of resolution and layer 4 representing the highest level of resolution. Let $\mathbf{p}_i(t)$ denote the function representing the approximation of the function $\mathbf{p}(t)$ resolution i . Then, $\mathbf{p}_4(t)$ is obtained by including wavelet coefficients for scales $0 \leq m \leq 4$, i.e., $f_4(x)$ is a summation of the form of Equation (5), with $M = 4$, as shown below in Equation (12).

Layer 3 data can be represented by dropping all wavelet coefficients corresponding to the finest scale used in the initial approximation $\mathbf{p}_4(t)$, resulting in the wavelet series shown in Equation (13); layer 2 data can be represented by dropping all wavelet coefficients corresponding to the finest scale in the layer 3 representation, resulting in the wavelet series of Equation (14); and so on. As scales are dropped from the wavelet approximation, the resolution of the approximation becomes progressively lower, i.e., the wavelet representation is effectively zooming out. Equations (12)-(16) show the wavelet synthesis equations for each layer.

$$\text{Layer 0:} \quad \mathbf{p}_0(t) \approx \sum_{i=-\infty}^{\infty} \mathbf{P}'(i) \psi_{0i}(x) + \sum_{m=0}^4 \sum_{i=-\infty}^{\infty} \mathbf{P}(m, i) \phi_{mi}(t) \quad (12)$$

$$\text{Layer 1:} \quad \mathbf{p}_1(t) \approx \sum_{i=-\infty}^{\infty} \mathbf{P}'(i) \psi_{0i}(x) + \sum_{m=0}^3 \sum_{i=-\infty}^{\infty} \mathbf{P}(m, i) \phi_{mi}(t) \quad (13)$$

$$\text{Layer 2:} \quad \mathbf{p}_2(t) \approx \sum_{i=-\infty}^{\infty} \mathbf{P}'(i) \psi_{0i}(x) + \sum_{m=0}^2 \sum_{i=-\infty}^{\infty} \mathbf{P}(m, i) \phi_{mi}(t) \quad (14)$$

$$\text{Layer 3:} \quad \mathbf{p}_3(t) \approx \sum_{i=-\infty}^{\infty} \mathbf{P}'(i) \psi_{0i}(x) + \sum_{m=0}^1 \sum_{i=-\infty}^{\infty} \mathbf{P}(m, i) \phi_{mi}(t) \quad (15)$$

$$\text{Layer 4:} \quad \mathbf{p}_4(t) \approx \sum_{i=-\infty}^{\infty} \mathbf{P}'(i) \psi_{0i}(x) + \sum_{i=-\infty}^{\infty} \mathbf{P}(0, i) \phi_{0i}(t) \quad (16)$$

Multi-resolution Error Metrics for Cartographic Databases

In addition to generating displayable maps, the wavelet coefficients of the cartographic data can be used to define a multi-resolution error metric for measuring database accuracy.

FIG. 8 illustrates a system 200 for generating a multi-resolution error metric in accordance with yet another embodiment of the present invention. The database which is being assessed for accuracy is commonly referred to as a sampled database 206. The system also includes another database called the ground truth database (DB) 204 and a processor 202. Both of these databases are shape point databases, i.e., both the sampled database 206 and the ground truth database 204 contain plural shape points and nodes representing the same geographic features, such as roads, and so forth; however, the shape points are more densely represented in the ground truth database 204 to give a highly accurate representation of the geographic features. The ground truth database is constructed by using more accurate sources (which may include preexisting maps or imagery, as well as sensor measurements) than those sources used for constructing the sampled database.

The processor 202 can be any computing device, including a conventional PC or other microprocessor-based device. The processor 202 can execute a computer software program for performing the steps shown in the flow chart diagram 230 of FIG. 9.

The flow chart diagram 230 illustrates a method of operating the processor 202 to generate one or more multi-resolution database error metrics. In step 232, the wavelet and scaling coefficients of the geographic features represented in the ground truth database are computed and stored in the ground truth wavelet database 204. This can be done by generating the coefficients from the shape points of the ground truth database (GD) on a per segment basis as described above in connection with FIGS. 1- 5.

The wavelet and scaling coefficients of the geographic features represented in the sampled database are then calculated and stored in the sampled wavelet database using the method as described above in connection with FIGS. 1- 5 (step 236).

The total error of the sampled database 206 with respect to the ground truth database 204 is designated $\mathbf{e}(t) = [e^x(t) \ e^y(t) \ e^z(t)]$, where $e^x(t)$, $e^y(t)$ and $e^z(t)$ are the components of error corresponding to longitude, latitude and altitude, respectively.

In step 238, the total error $\mathbf{e}(t)$ is computed as follows:

$$\begin{aligned}\mathbf{e}(t) &= \sum_{i=-\infty}^{\infty} [\mathbf{P}'_{SD}(i) - \mathbf{P}'_{GD}(i)] \phi_{M'i}(t) + \sum_{m=M'}^M \sum_{i=-\infty}^{\infty} [\mathbf{P}_{SD}(m,i) - \mathbf{P}_{GD}(m,i)] \psi_{mi}(t) \\ &= \mathbf{e}_{M'}(t) + \sum_{m=M'}^{\infty} \mathbf{e}_m(t)\end{aligned}\quad (17)$$

where

$$\begin{aligned}\mathbf{e}_{M'}(t) &= \sum_{i=-\infty}^{\infty} [\mathbf{P}'_{SD}(i) - \mathbf{P}'_{GD}(i)] \phi_{M'i}(t) + \sum_{i=-\infty}^{\infty} [\mathbf{P}_{SD}(M',i) - \mathbf{P}_{GD}(M',i)] \psi_{M'i}(t) \\ \mathbf{e}_m(t) &= \sum_{i=-\infty}^{\infty} [\mathbf{P}_{SD}(m,i) - \mathbf{P}_{GD}(m,i)] \psi_{mi}(t), \text{ for } M' < m \leq M\end{aligned}\quad (18)$$

and \mathbf{P}_{GD} and \mathbf{P}_{SD} are the wavelet coefficients of the ground truth database 204 and the sampled database 206, respectively and \mathbf{P}'_{GD} and \mathbf{P}'_{SD} are the scaling coefficients of the ground truth database 204 and the sampled database 206, respectively. The set of values $\{\mathbf{e}_m(t) = [e_m^x(t) \ e_m^y(t) \ e_m^z(t)]\}$ represent the layer error metric values.

In step 240, a layer error metric value can be generated for a selected resolution layer of the sampled database 206. The total error determined by Equation (14) is thus decomposed into error components at different scales, represented by the integer m . Thus two types of error can be obtained for each geographic feature represented in the sampled database: the layer error $\mathbf{e}_m(t)$ at a particular scale m , as well as the total error $\mathbf{e}(t)$, which is the sum of the errors at all scales. Note that $\mathbf{e}_m(t)$ and $\mathbf{e}(t)$ are vectors, with longitude, latitude and altitude components.

But we can compute $e_m^{combined}(t) = (e_m^x(t)^2 + e_m^y(t)^2 + e_m^z(t)^2)$ and $e^{combined}(t) = (e^x(t)^2 + e^y(t)^2 + e^z(t)^2)$ to get a combined measure of error in all three directions.

In step 242, the values of the error metric are stored by the processor 202 for later analysis and use by a computer system.

Conclusion

Wavelets are useful for yielding a compact representation of cartographic data with improved accuracy, and for line generalization, and zooming. Furthermore, different wavelet bases can be applied to a cartographic database, once the initial wavelet formulation has been done. Moreover, the wavelet transform can be extended to two or more dimensions according to teachings disclosed herein. For instance, a two-dimensional wavelet representation of geographical information can be used to represent surfaces.

While specific embodiments of the present invention have been shown and described, it will be apparent to those skilled in the art that the disclosed invention may be modified in numerous ways and may assume many embodiments other than those specifically set out and described above. Accordingly, the scope of the invention is indicated in the appended claims, and all changes that come within the meaning and range of equivalents are intended to be embraced therein.

WHAT IS CLAIMED IS:

1 1. A method for representing cartographic data in a computer-based system,
2 comprising:
3 computing a plurality of wavelet and scaling coefficients corresponding to at
4 least one function representing a geographic feature in a cartographic database; and
5 storing the wavelet and scaling coefficients in a computer-usable database, the
6 coefficients being usable for representing the cartographic data in the computer-based system.
7

1 2. The method of claim 1, wherein the geographic feature is originally represented
2 by a plurality of data points.

1 3. The method of claim 2, wherein the data points are selected from the group
2 consisting of coordinate pairs and a coordinate triples.

1 4. The method of claim 1, wherein the geographic feature is the boundary of a
2 feature selected from the group consisting of a road, waterway, building, park, lake, railroad
3 track, and airport.
4

1 5. The method of claim 2, wherein the step of computing the wavelet coefficients
2 and scaling coefficients includes applying a wavelet transform to a function defined by the data
3 points representing the geographic feature.
4

1 6. The method of claim 1, wherein the step of computing the wavelet coefficients
2 and scaling coefficients includes:
3 computing the wavelet coefficients by performing a least-squares fit.
4

1 7. The method of claim 1, wherein the wavelet and scaling coefficients are
2 computed using a semi-discrete orthonormal wavelet transform.

1 8. A method of displaying on a computer output device a function representing a
2 geographic feature, comprising:
3 retrieving from a computer-usable database a plurality of wavelet and scaling
4 coefficients associated with the geographic feature, the coefficients being derived from a
5 plurality of data points specifying geographic locations according to a predetermined reference
6 system;
7 computing the function using the retrieved wavelet and scaling coefficients; and
8 displaying the function on the computer output device.
9

1 9. The method of claim 8, wherein the data points are selected from the group
2 consisting of coordinate pairs and a coordinate triples.

1 10. The method of claim 8, wherein the geographic feature is selected from the group
2 consisting of a road, waterway, building, park, lake, railroad track, and airport.
3

1 11. A system for displaying on a computer output device a representation of a
2 geographic feature, comprising:
3 a database storing a plurality of wavelet and scaling coefficients associated with
4 the geographic feature, the wavelet and scaling coefficients being derived from a plurality of
5 data points specifying geographic locations according to a predetermined reference system;
6 a processor configured to calculate a function using the wavelet and scaling
7 coefficients, the function representing the geographic feature; and
8 a display device for displaying the function.
9

1 12. The system of claim 11, wherein the data points are selected from a group
2 consisting of coordinate pairs and coordinate triples.
3

1 13. A method of generating a computer-usable database that represents cartographic
2 data using a plurality of wavelet and scaling coefficients, comprising:
3 providing a predetermined database that represents the cartographic data using a
4 plurality of data points specifying geographic locations;
5 computing a plurality of wavelet and scaling coefficients from the data points; and
6 storing the wavelet and scaling coefficients in the computer-usable database.
7

1 14. The method of claim 13, wherein the data points are selected from the group
2 consisting of coordinate pairs and coordinate triples.

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1 19. The system of claim 16, wherein the wavelet coefficients are computed by
2 performing a least-squares fit.

1 20. A method for generating a database error metric in a computer-based system,
2 comprising:
3 computing a first plurality of wavelet and scaling coefficients from a plurality of
4 first data points included in a first cartographic database;
5 computing a second plurality of wavelet and scaling coefficients from a plurality
6 of data points included in a second cartographic database; and
7 generating the database error metric based on a wavelet transform involving the
8 first and second pluralities of wavelet coefficients.

1 21. The method of claim 20, wherein the error metric is a total error metric based on a
2 plurality of wavelet scales.

1 22. The method of claim 20, further comprising:
2 selecting a wavelet scale; and
3 restricting the error computation to the selected wavelet scale to generate a layer
4 error metric.

1 23. The method of claim 14, wherein the data points are selected from the group
2 consisting of coordinate pairs and coordinate triples.

1 24. A system for generating a database error metric, comprising:
2 a first cartographic database for storing a first plurality of data points;
3 a second cartographic database for storing a second plurality of data points; and
4 a processor, operatively coupled to the first and second cartographic databases,
5 configured to compute a first plurality of wavelet and scaling coefficients and a second plurality
6 of wavelet and scaling coefficients, respectively, from the first and second pluralities of data
7 points, the processor generating a database error metric based on the first and second pluralities
8 of wavelet and scaling coefficients.

1 25. The system of claim 23, wherein the error metric is a total error metric based on a
2 plurality of wavelet scales.

1 26. The system of claim 24, wherein the processor is configured to restrict the error
2 computation to a selected wavelet scale to generate a layer error metric.

1 27. The system of claim 24, wherein the data points are selected from the group
2 consisting of coordinate triples and coordinate pairs.

METHOD AND SYSTEM FOR WAVELET-BASED REPRESENTATION AND USE OF CARTOGRAPHIC DATA

5 ABSTRACT OF THE DISCLOSURE

Cartographic data is represented using wavelet coefficients. Specifically, a cartographic shape point database consisting of shape points and nodes stored on a per geographic feature basis is converted to a cartographic wavelet database consisting of wavelet and scaling coefficients also stored on a per geographic feature basis. The shape of each geographic feature can be reconstructed from the stored wavelet and scaling coefficients for that geographic feature. The wavelet transform organizes the information in a function according to scale, a concept which is related to resolution. The wavelet-based representation facilitates operations such as line simplification (generalization) and zooming. Multi-resolution error metrics are defined using the wavelet representation for assessing the accuracy of sampled cartographic databases with respect to a ground truth database.

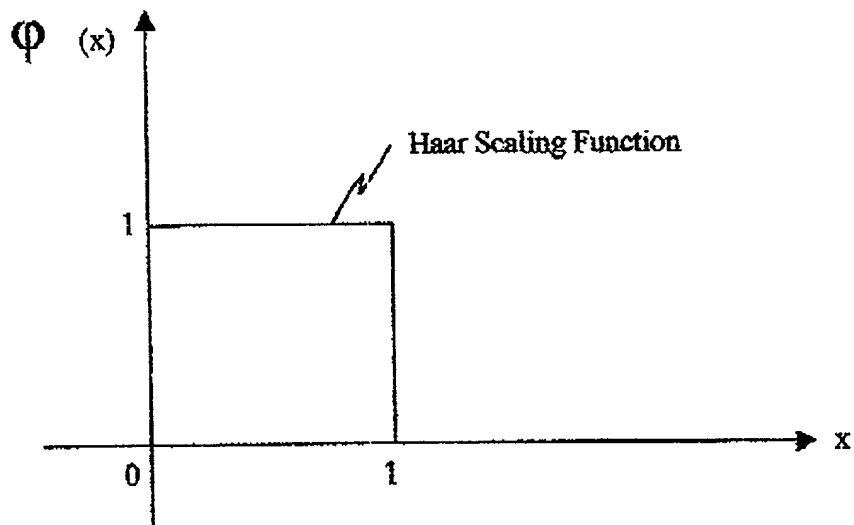
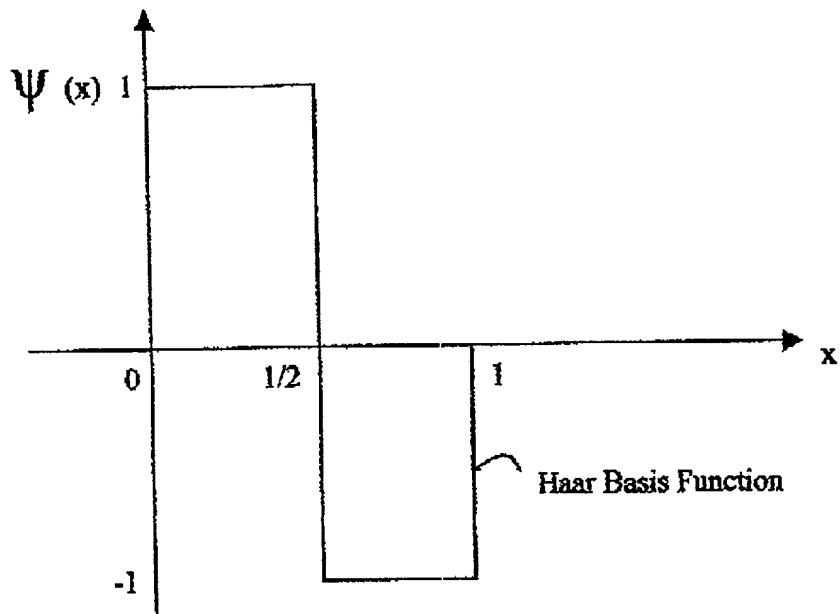


FIG. 1

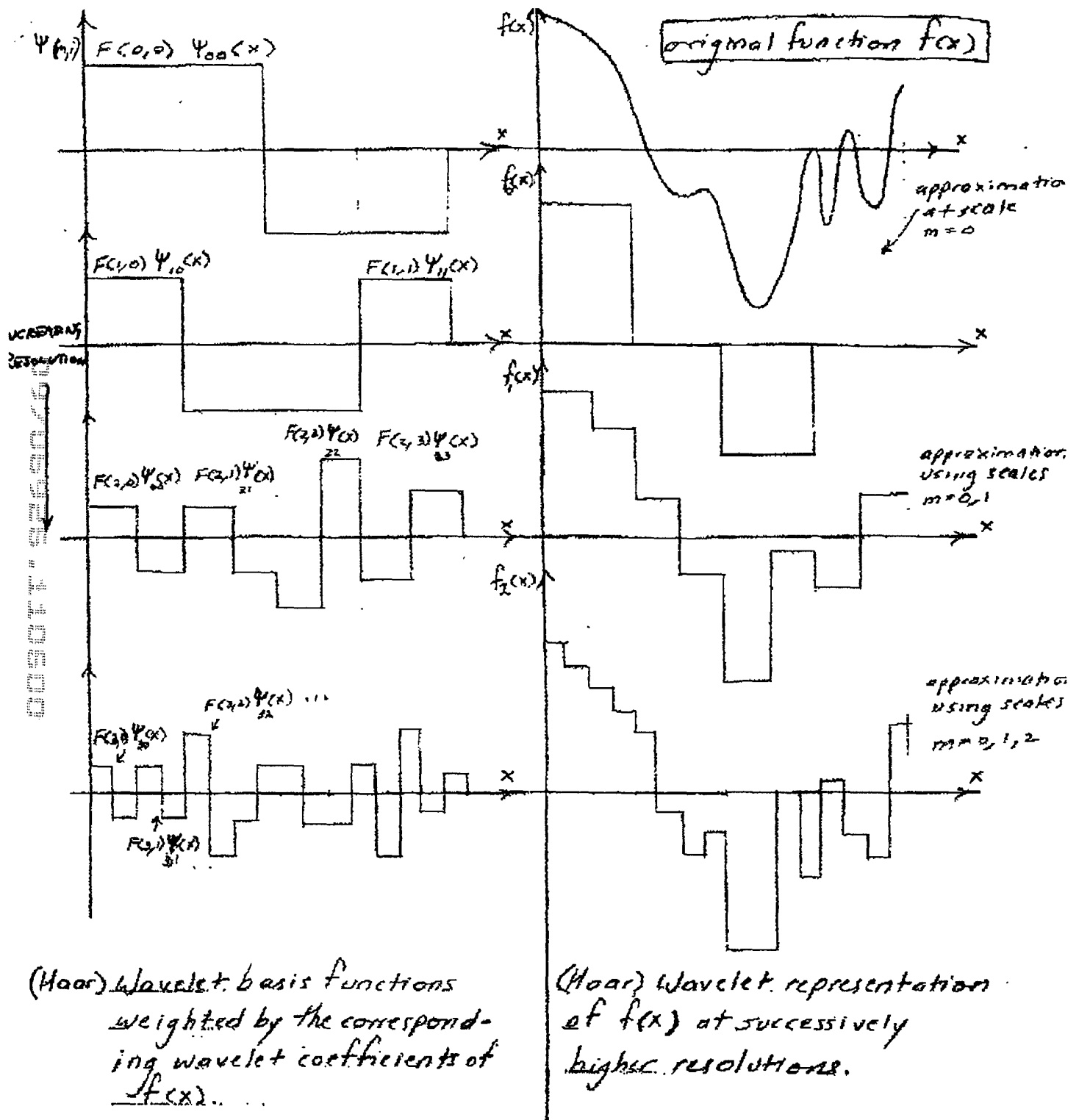
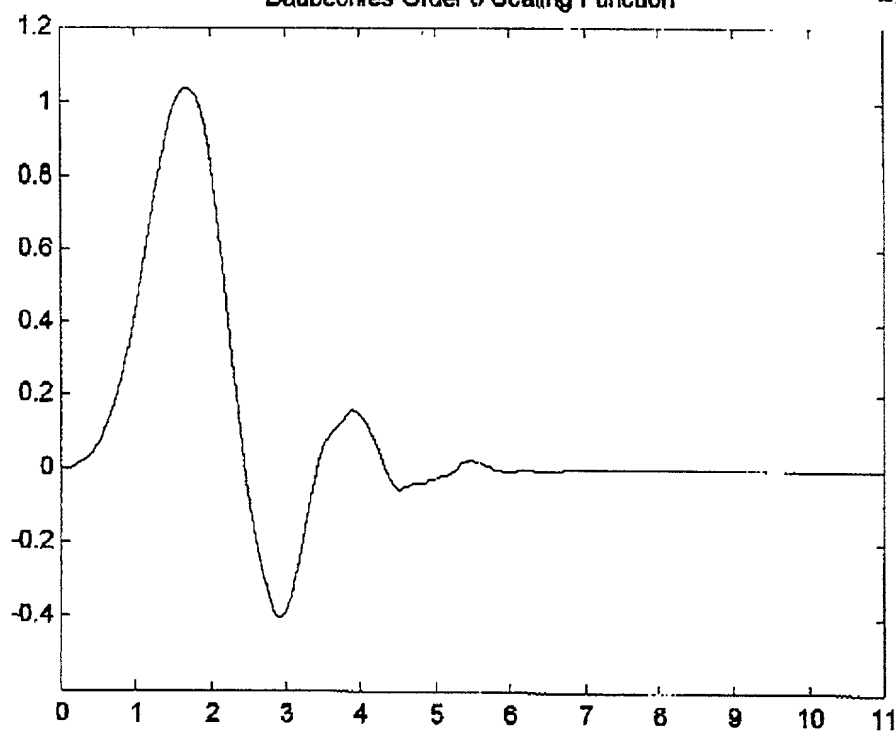


Fig. 2

Daubechies Order 6 Scaling Function



Daubechies Order 6 Basis Function

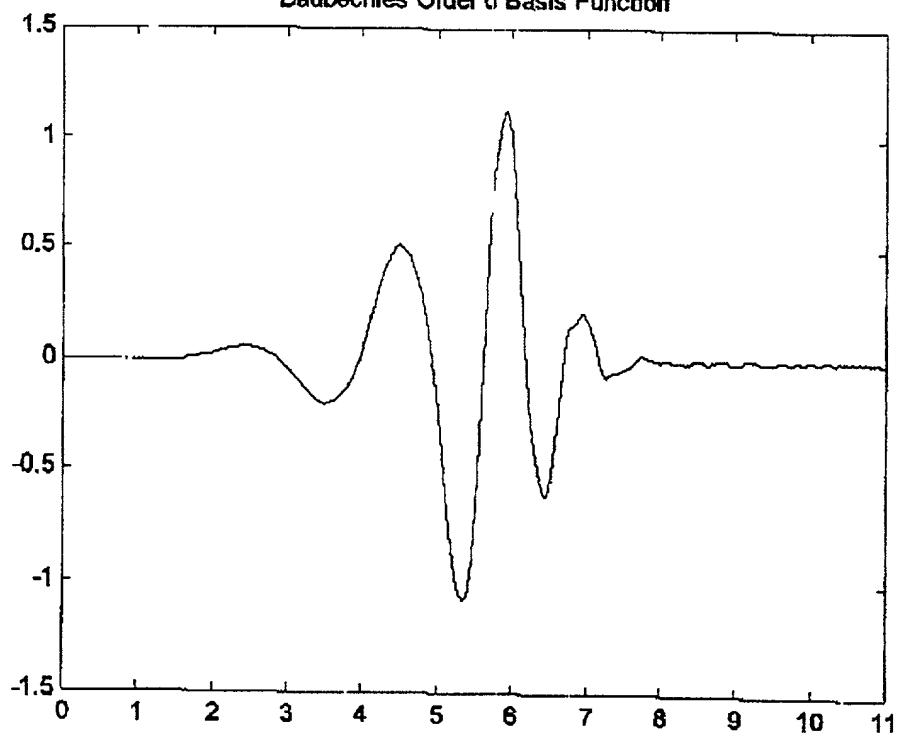


FIG. 3

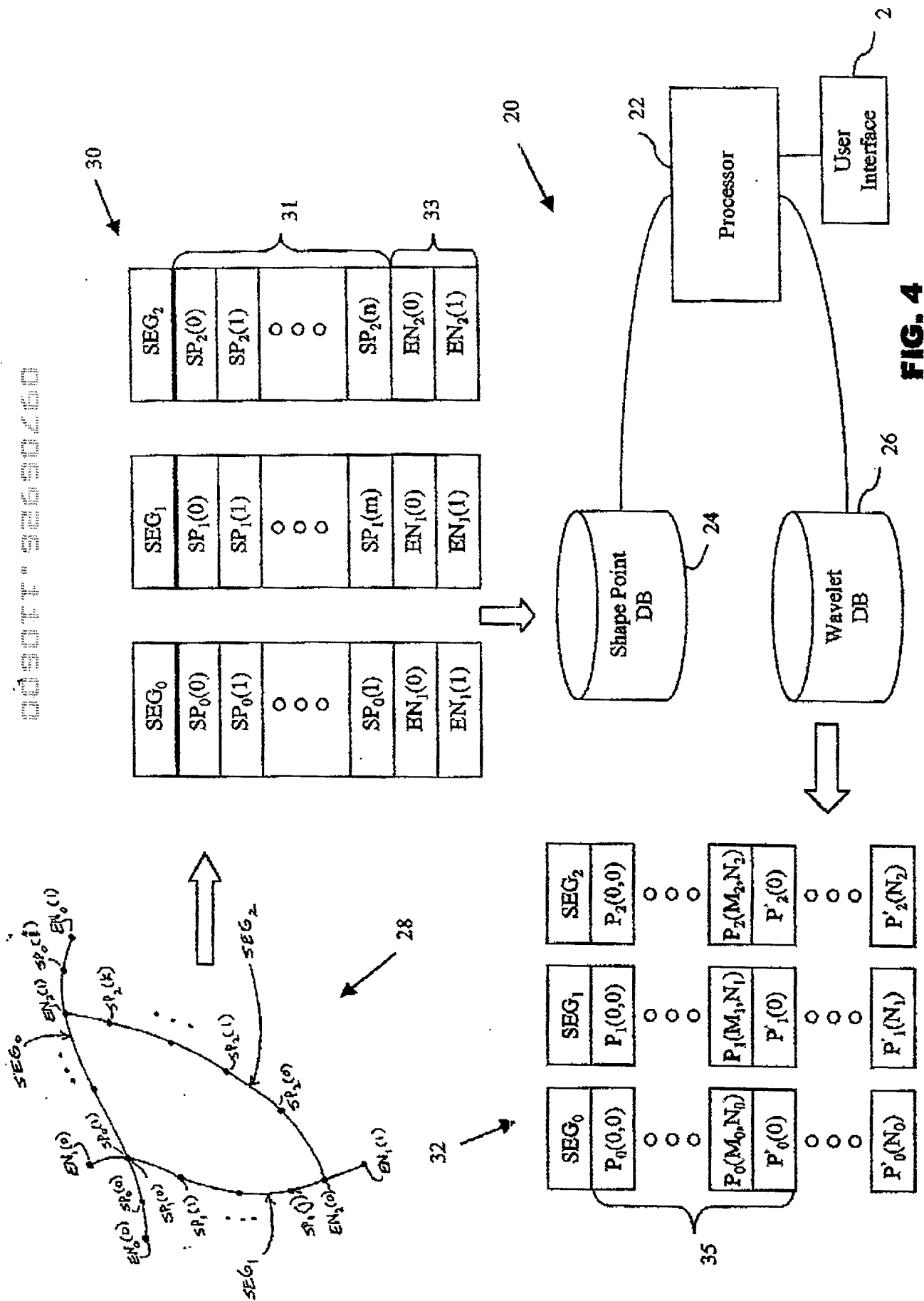


FIG. 4

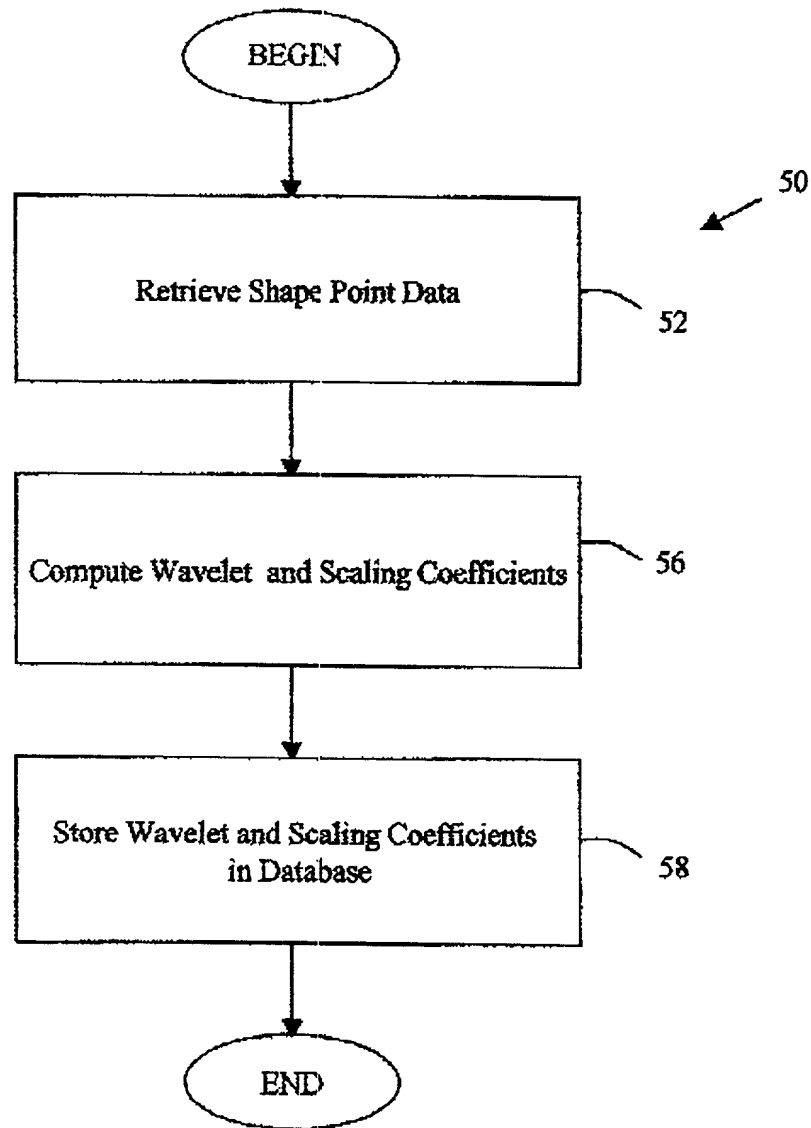


FIG. 5

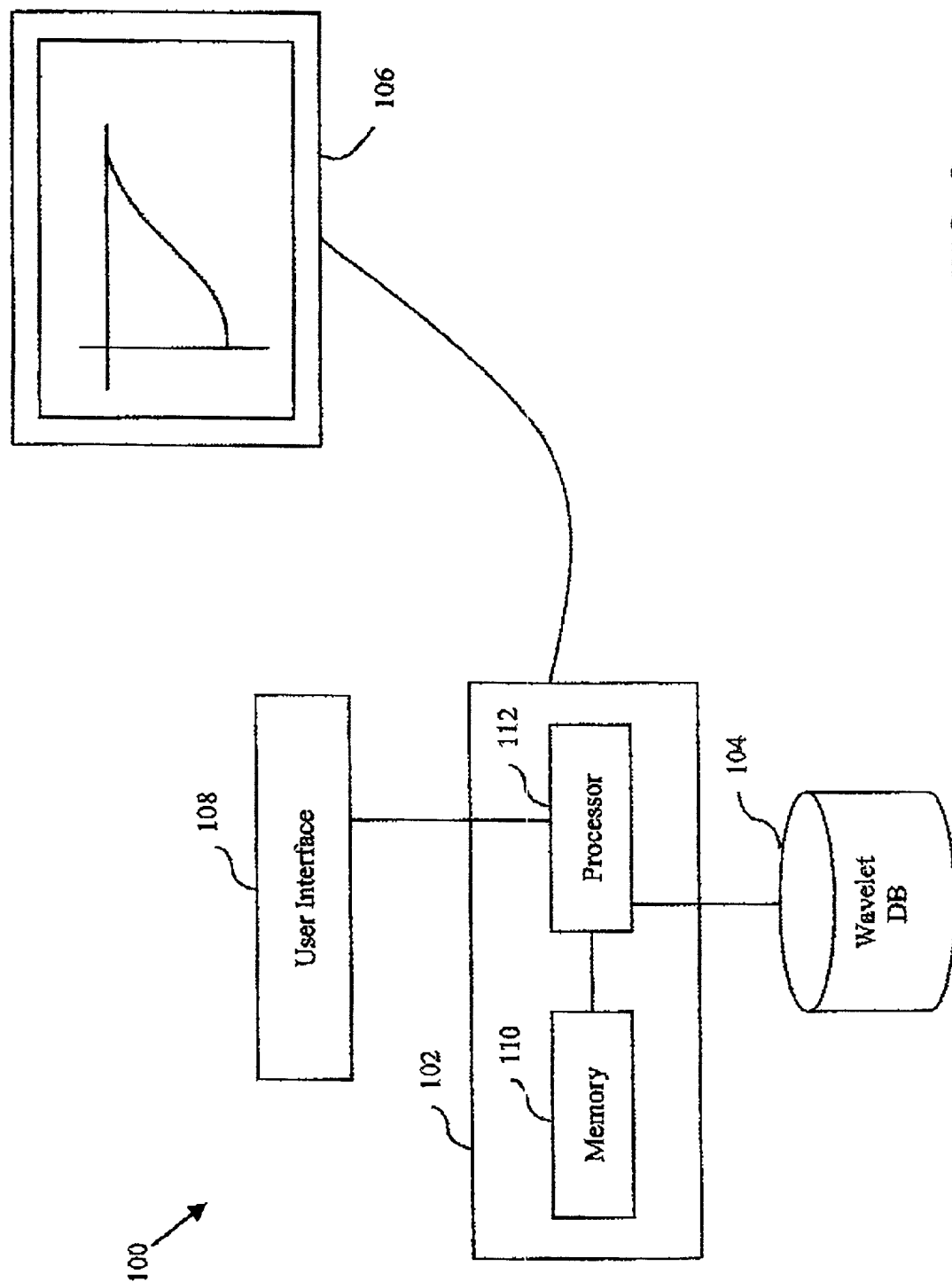


FIG. 6

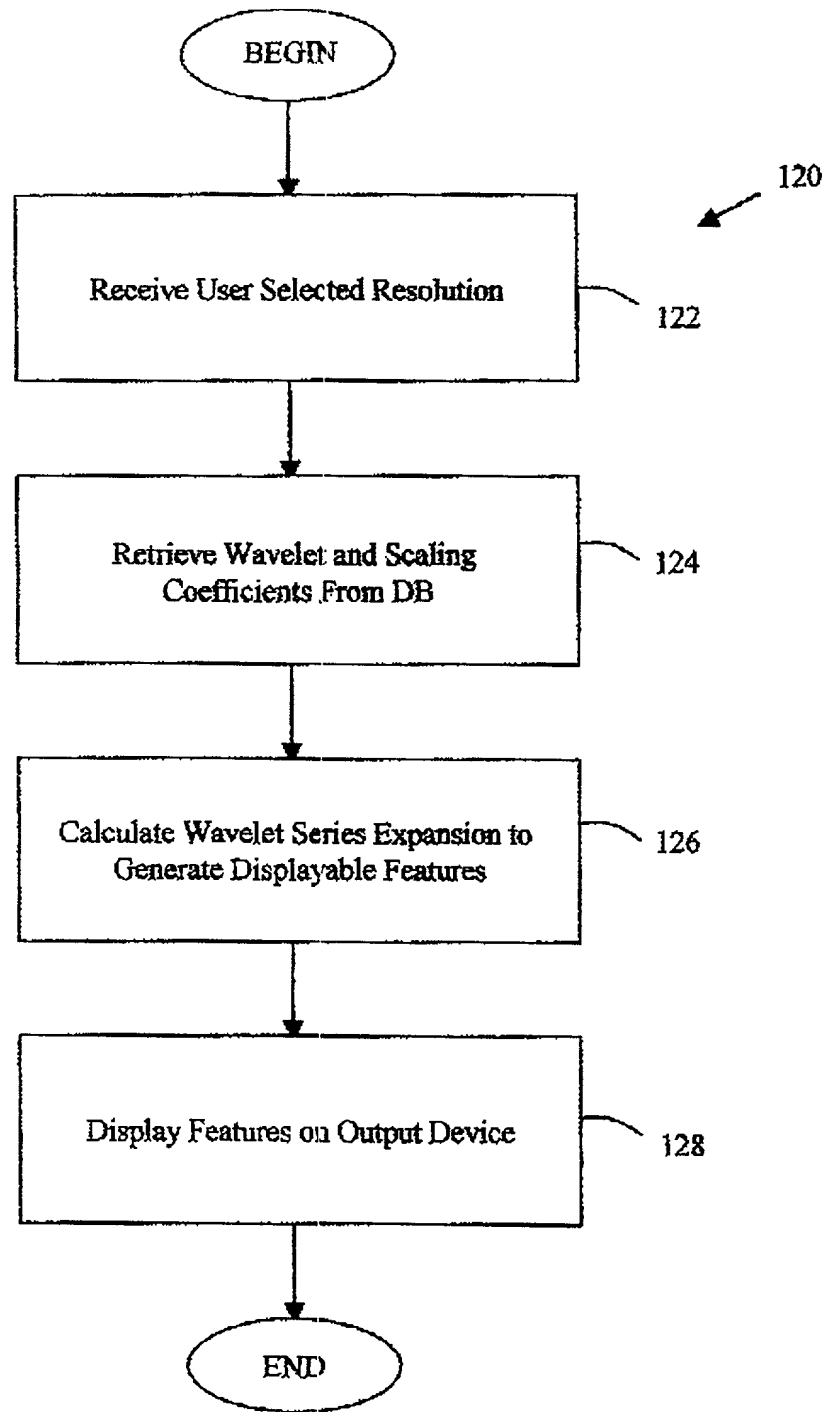


FIG. 7

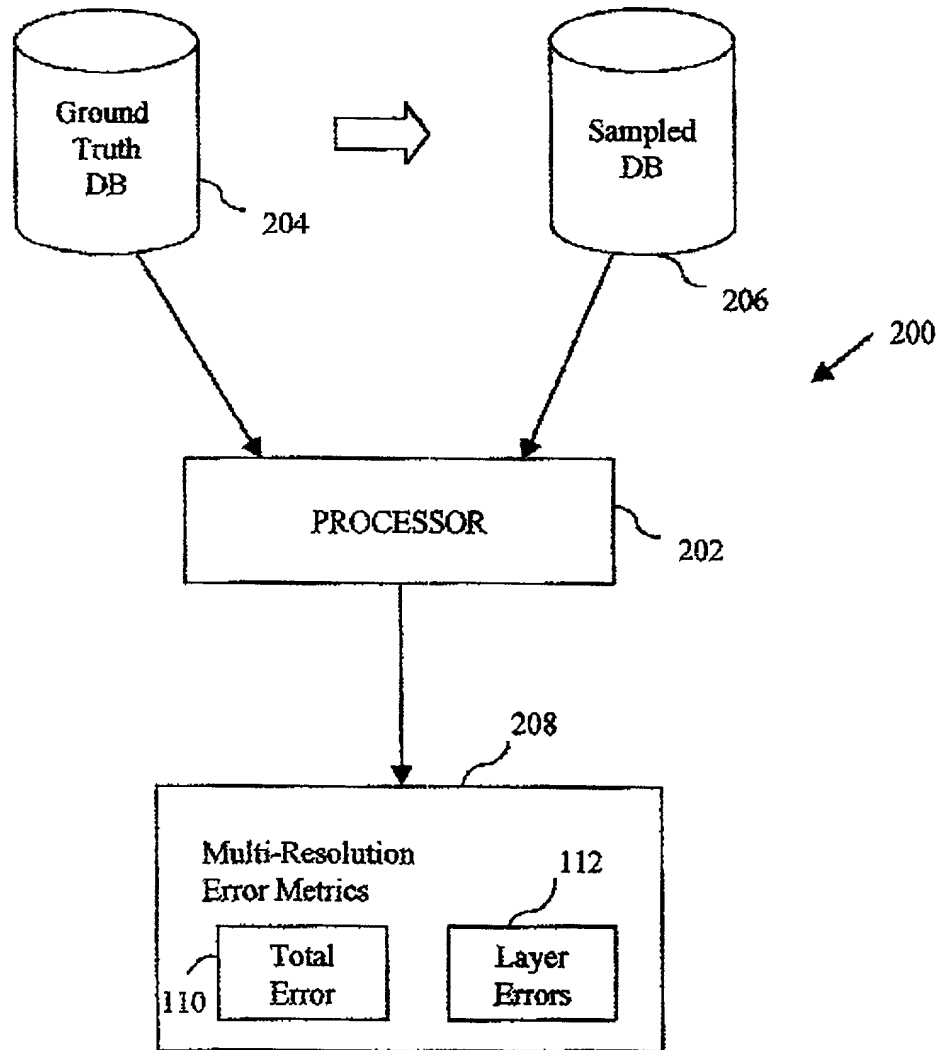


FIG. 8

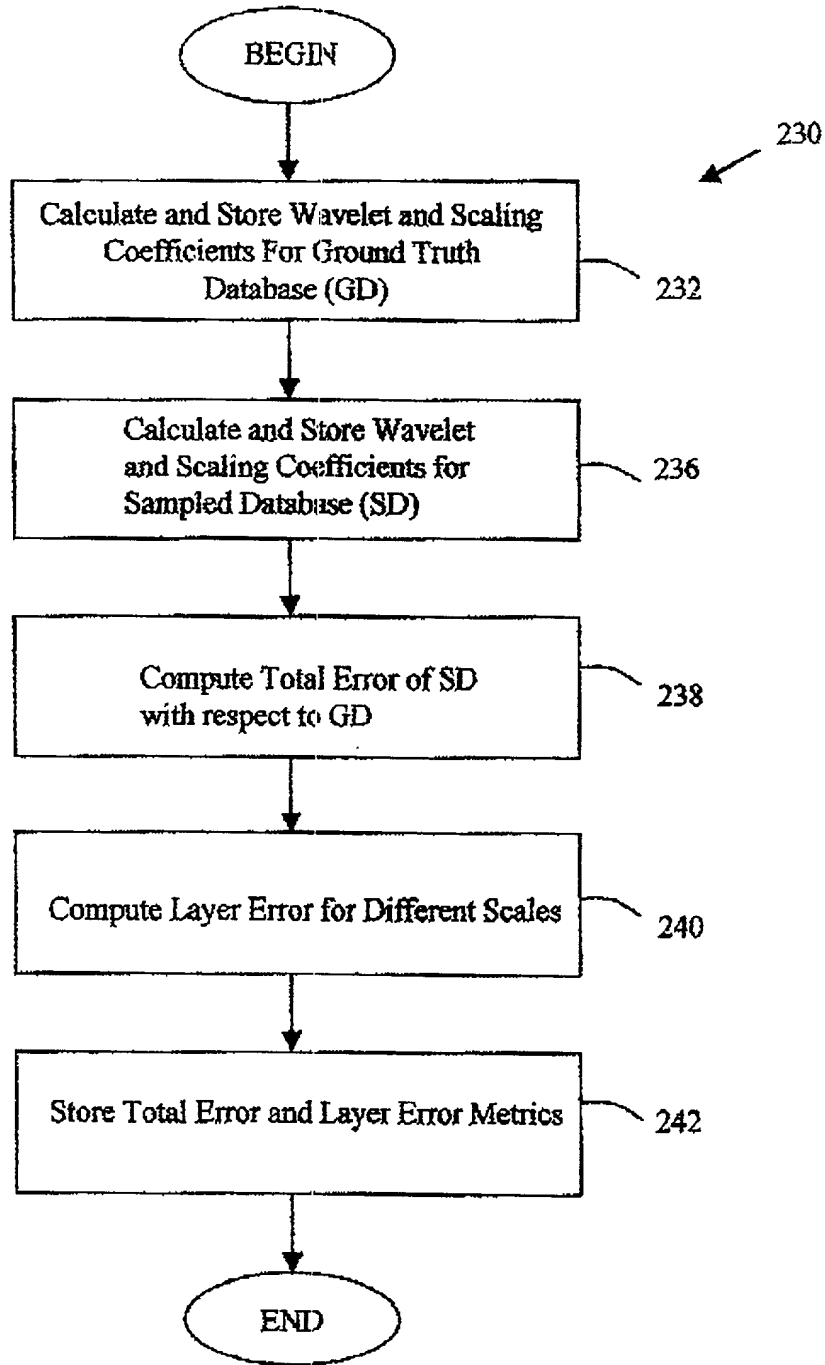


FIG. 9

DECLARATION FOR PATENT APPLICATION

As a below named inventor, I hereby declare that:

My residence, post office address and citizenship are as stated below next to my name.

I believe I am the original, first and sole inventor (if only one name is listed below) or an original, first and joint inventor (if plural names are listed below) of the subject matter which is claimed and for which a patent is sought on the invention entitled, METHOD AND SYSTEM FOR WAVELET-BASED REPRESENTATION AND USE OF CARTOGRAPHIC DATA, the specification of which:

- ☒ is attached hereto.
☐ was filed on _____ as Application Serial No. _____.
☐ and was amended on _____ (if applicable).

I hereby state that I have reviewed and understand the contents of the above-identified specification, including the claims, as amended by any amendment referred to above.

I acknowledge the duty to disclose information which is material to the patentability as defined in Title 37, Code of Federal Regulations, § 1.56(a).

I hereby claim foreign priority benefits under 35 U.S.C. § 119(a)-(d) or § 365(b) of any foreign application(s) for patent or inventor's certificate or § 365(a) of any PCT International application which designated at least one country other than the United States, listed below and have also identified below, by checking the box, any foreign application for patent or inventor's certificate, or PCT International application having a filing date before that of the application on which priority is claimed:

<u>Prior Foreign Application(s)</u>			<u>Priority Claimed</u>	
_____	_____	_____	<input type="checkbox"/>	<input type="checkbox"/>
(Number)	(Country)	(Day/Month/Year Filed)	Yes	No

I hereby claim the benefit under 35 U.S.C. § 119(e) of any United States provisional application(s) listed below:

_____	_____
(Application Serial No.)	(Filing Date)

I hereby claim the benefit under 35 U.S.C. § 120 of any United States application(s), or § 365(c) of any PCT International application designating the United States, listed below and, insofar as the subject matter of each of the claims of this application is not disclosed in the prior United States or PCT International application in the manner provided by the first paragraph of 35 U.S.C. § 112, I acknowledge the duty to disclose information which is material to patentability as defined in 37 CFR § 1.56 which became available between the filing date of the prior application and the national or PCT International filing date of this application:

_____	_____	None
(Application Serial No.)	(Filing Date)	(Status-patented, pending, abandoned)

As a named inventor, I hereby appoint the following registered practitioners to prosecute said patent application and to transact all business in the Patent and Trademark Office connected therewith:

Frank J. Kozak (Reg. No. 32,908)
 Lawrence M. Kaplan (Reg. No. 33,521)

Direct all correspondence for the above-identified application and telephone calls to:

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 fax: (847) 795-7228

I hereby declare that all statements made herein of my own knowledge are true and that all statements made on information and belief are believed to be true; and further that these statements were made with the knowledge that willful false statements and the like so made are punishable by fine or imprisonment, or both, under Section 1001 of Title 18 of the United States Code and that such willful false statements may jeopardize the validity of the application or any patent issued thereon.

Inventor's Signature

Full name of sole or first inventor

Residence

Citizenship

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Rajashri R. Joshi

Date:

11/06/2000RAJASHRI JOSHISCHAUMBURG, ILLINOISCANADIAN2504 JESSICA LN, #127, SCHAUMBURG, IL 60173

rev. Feb. 1999